## 5.4 - Medians and Altitudes in Triangles

1) Construct the orthocenter of the triangle.

2) Construct the centroid of the triangle.


In $\triangle A B C, X$ is the centroid.
3) If $C W=15$, find $C X$ and $X W$.

$$
\begin{aligned}
& c x=10 \\
& x w=5
\end{aligned}
$$

4) If $B X=8$, find $B Y$ and $X Y$.

$$
\begin{aligned}
& B y=12 \\
& x y=4
\end{aligned}
$$

5) If $X Z=3$, find $A X$ and $A Z$.

$$
\begin{aligned}
& A X=6 \\
& A Z=9
\end{aligned}
$$

Is $\overline{A B}$ a median, an altitude, or neither? Explain.
6)


Median. $\overline{A B}$ bisects the opposite side.
7) $A$


Altitude. $\overline{A B}$ is 1 to the opposite side.
9)


Neither. $\overline{A B}$ is neither 1 nor does it bisect the opposite side.
10) Name the centroid.


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Patio
11) Name the orthocenter.


In the following, name indicated segment
12) a median in $\triangle A B C$

$$
\overline{C J}
$$

13) an altitude for $\triangle A B C$

FF
14) a median in $\triangle A H C$
$\overline{1 H}$
15) an altitude for $\triangle A H B$
$\overline{A H}$
16) an altitude for $\triangle A H G$

17) Point $M$ is the centroid

$$
C M=16
$$

$$
M O=10
$$

$$
T S=21
$$

$$
A M=20
$$

$S M=$ $\qquad$
$T M=$ $\qquad$

$U M=$ $\qquad$
19) Point $Z$ is the centroid

18) Point $S$ is the centroid

$$
\begin{aligned}
& D S=8 \\
& L S=18 \\
& E S=G S+4 \\
& G S=16 \\
& O S=\frac{10}{9} \\
& N S=9
\end{aligned}
$$


20) Point $G$ is the centroid

$$
\begin{aligned}
& G I=G R=G N \\
& E R=36 \\
& B G=24 \\
& I G=12
\end{aligned}
$$


21) Identify each statement as describing the incenter, circumcenter, orthocenter, or centroid.
a. $\qquad$ The point equally distant from the three sides of a triangle.
b. $\qquad$ The point equidistant from the three vertices.
c. Circumcenter The intersection of the perpendicular bisectors of the sides of a triangle.
d. Orthocenter The intersection of the altitudes of a triangle.
e. $\qquad$ The intersection of the angle bisectors of a triangle.
f. $\qquad$ The intersection of the medians of a triangle.
g. $\qquad$ The midpoint on the hypotenuse of a right triangle.
h. $\qquad$ The point at a vertex of a right triangle.
22) A circular revolving sprinkler needs to be set up to water every part of a triangular garden. Describe where the sprinkler should be located so that it reaches all the corners of the garden?

23) You need to supply electric power to three transformers, one on each of three roads enclosing a large triangular track of land. Each transformer should be the same distance from the power-generation plant and as close to the plant as possible. Sketch a figure and describe where you should build the power plant, and where should you locate each transformer?

24) Birdy wishes to decorate her glider with the largest possible circle within her large triangular hang glider. She needs to locate which point of concurrency?


